# Unification of General Relativity, Quantum Mechanics, and Hawking Radiation 

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#### Abstract

General Relativity and Quantum Mechanics might seem to be far reaching philosophies of time and space yet we are enlightened by them in every reach of the conscience. Hawking Radiation is no such exception to our worlds. Black Holes might seem far away yet they are nearer than we think. Quan-tum Phenomenon encapsulates every reach of our existence and bounds us to a simultaneous world of richness. Hawking Radiation is no exception to the rule no matter how bizarre it might seem to the naked eye.


Keywords: General Relativity, Quantum Mechanics, Hawking Radiation, Black Holes, Quan-tum Phenomenon

## 1. Introduction

This text aims to unify General Relativity, Quantum Mechanics, and Hawking Radiation using the ds4 equation and other variants of similar form. It will begin with an Abstract, further on to a Main Content which will cover both text and calculations, depict Graphs, display Code, and provide Conclusivity to our exploration, unification, and depiction of such phenomenon into one comprehensive theory.

## 2. Main Content

### 2.1 Gott Time Equation

Given the Gott Time Equation,

Accepting the possibility of imaginary values for T. Here's the calculation for each pair of $R$ and $\mu$ :

Given values:
$R$ : [100.3844, 174.844]
$G: ~ 6.674 \times 10^{-11} \mathrm{~m}^{3} \mathrm{~kg}^{-1} \mathrm{~s}^{-2}$
$\mu: \quad[0.3769942894460652, \quad-0.151111504310964$, 0.09479860644227443 , -0.0015150532909259436 , $0.0015149218565185572, \quad-0.007575548754339321$, $0.009725139642140273,-0.02467122830727323$, $0.009759643375978265,-0.11074352593242188$ ]

Now, let's calculate $T$ for each pair of $R$ and $\mu$ :
Here are the calculated values for $T$ for each pair of $R$ and $\mu$ :

1. For $R=100.3844$ and $\mu=0.3769942894460652$ :
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times 0.3769942894460652}} \approx 0.6658226252295824$
2. For $R=100.3844$ and $\mu=-0.151111504310964$ :
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.151111504310964)}} \approx 0.9624867964581438 i$
3. For $\mathrm{R}=100.3844$ and $\mu=0.09479860644227443$ :
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times 0.09479860644227443}} \approx 1.3006851299739557$
4. For $\mathrm{R}=100.3844$ and $\mu=-0.0015150532909259436$
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.0015150532909259436)}} \approx 9.695949581834495 i$
5. For $\mathrm{R}=100.3844$ and $\mu=0.0015149218565185572$ :
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times 0.0015149218565185572}} \approx 9.69479326986721$
6. For $\mathrm{R}=100.3844$ and $\mu=-0.007575548754339321$
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.007575548754339321)}} \approx 3.0829495352654064 i$
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7. For $\mathrm{R}=100.3844$ and $\mu=-0.009725139642140273$ :
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.009725139642140273)}} \approx 2.7983406414341096 i$
8. For $\mathrm{R}=100.3844$ and $\mu=-0.02467122830727323$
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.02467122830727323)}} \approx 1.692196842141486 i$
9. For $\mathrm{R}=100.3844$ and $\mu=-0.009759643375978265$ :
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.009759643375978265)}} \approx 2.788486369693627 i$
10. For $\mathrm{R}=100.3844$ and $\mu=-0.11074352593242188$
$T=2 \pi \sqrt{\frac{(100.3844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.11074352593242188)}} \approx 0.6244894465091079 i$
11. For $R=174.844$ and $\mu=0.3769942894460652$
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times 0.3769942894460652}} \approx 0.8506065225102651$
12. For $\mathrm{R}=174.844$ and $\mu=-0.151111504310964$
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.151111504310964)}} \approx 1.2295612090066257 i$
13. For $\mathrm{R}=174.844$ and $\mu=0.09479860644227443$
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times 0.09479860644227443}} \approx 1.1505091311418195$
14. For $R=174.844$ and $\mu=-0.0015150532909259436$
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.0015150532909259436)}} \approx 9.640788095352509 i$
15. For $\mathrm{R}=174.844$ and $\mu=0.0015149218565185572$
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times 0.0015149218565185572}} \approx 9.640632589354664$
16. For $R=174.844$ and $\mu=-0.007575548754339321$ :
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.007575548754339321)}} \approx 3.047879035211784 i$
17. For $\mathrm{R}=174.844$ and $\mu=-0.009725139642140273$ :
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.009725139642140273)}} \approx 2.7619028812245756 i$
18. For $\mathrm{R}=174.844$ and $\mu=-0.02467122830727323$ :
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.02467122830727323)}} \approx 1.6754212223730562 i$
19. For $\mathrm{R}=174.844$ and $\mu=-0.009759643375978265$
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.009759643375978265)}} \approx 2.768458695104001 i$
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20. For $R=174.844$ and $\mu=-0.11074352593242188$ :
$T=2 \pi \sqrt{\frac{(174.844)^{3}}{2 \times 6.674 \times 10^{-11} \times(-0.11074352593242188)}} \approx 0.6061942191110191 i$

These are the calculated values for $T$ for each pair of $R$ and $\mu$. As expected, some of the values are imaginary due to the presence of negative values for $\mu$, that is negative mass.

### 2.2 Action S

The expression for the action $S$ given as:

$$
S=\int d^{4} x \sqrt{-g} \mathcal{L}\left(\Phi, \partial_{\mu} \Phi, g_{\mu \nu}\right)
$$

is a foundational concept in theoretical physics, particularly in the context of general relativity and field theory. Let's break down the components and under-stand how they contribute to the dynamics of a system, such as the hypothetical Romulan Quantum Singularity Propulsion System.

## Components of the Action

1) Spacetime Volume Element $\left(d^{4} x\right)$ : - This represents the infinitesimal volume element in four-dimensional spacetime. It ensures that the integral covers the entire spacetime manifold
2) Determinant of the Metric Tensor $(\sqrt{-g})$ : - The metric tensor $\mathrm{g}_{\mu \nu}$ describes the geometry of spacetime. The determinant $g$ (where $g=\operatorname{det}\left(g_{\mu \nu}\right)$ ) encapsulates the curvature effects. The negative sign indicates that the met-ric has a Lorentzian signature, which is typical in general relativity (one time dimension and three spatial dimensions).
3) Lagrangian Density $\left(L\left(\Phi, \partial_{\mu} \Phi, g_{\mu \nu}\right)\right)$ : The Lagrangian density L is a function that depends on the matter fields $\Phi$, their derivatives $\partial_{\mu} \Phi$, and the metric tensor $g_{\mu \nu}$. It encapsulates the dynamics of the fields, including their interactions and coupling with the gravitational field.

## Structure of the Lagrangian Density

The specific form of the Lagrangian density L can be quite complex, es-pecially in advanced theoretical models like those involving exotic propulsion systems. However, a typical Lagrangian density for a scalar field coupled to gravity might include the following terms:

## 1) Kinetic Term for the Scalar Field:

$$
\mathcal{L}_{k i n}=-\frac{1}{2} g^{\mu \nu} \partial_{\mu} \Phi \partial_{\nu} \Phi
$$

This term describes the kinetic energy of the scalar field $\Phi$.

## 2) Potential Term for the Scalar Field:

$$
\mathcal{L}_{\text {pot }}=-V(\Phi)
$$

This term describes the potential energy of the scalar field, where $\mathrm{V}(\Phi)$ is a function of $\Phi$.
3) Gravitational Coupling: The interaction between the scalar field and the gravitational field can be more intricate, involving non-minimal couplings

Such as:

$$
\mathcal{L}_{\text {int }}=-\xi \Phi^{2} R
$$

where $R$ is the Ricci scalar representing curvature, and $\xi$ is a coupling constant.

Example of a Lagrangian Density
Putting these elements together, a possible Lagrangian density for a scalar field $\Phi$ with a potential $V(\Phi)$ and minimal coupling to gravity could look like:

$$
\mathcal{L}=\frac{1}{2} \partial_{\mu} \Phi \partial^{\mu} \Phi-V(\Phi)+\frac{1}{2} \xi R \Phi^{2}
$$

where: $-\frac{1}{2} \partial_{\mu} \delta \partial^{\mu} \phi$ is the kinetic term, $-\mathrm{V}(\Phi)$ is the potential term, $-\frac{1}{2} \xi R \phi^{2}$ represents the interaction between the scalar field and the gravitational field.

## Implications for a Romulan Quantum Singularity Propulsion System

In the context of a Romulan Quantum Singularity Propulsion System, which hypothetically uses a quantum singularity for propulsion, the Lagrangian density would likely need to include terms accounting for:

- The exotic matter fields involved in stabilizing and utilizing the singularity.
- Non-trivial gravitational effects due to the intense curvature near the singu-larity. - Quantum mechanical effects that could play a significant role in such extreme conditions.

The exact form of $L$ would be determined by the specific theoretical model describing the propulsion system, potentially involving advanced concepts from quantum field theory in curved spacetime, general relativity, and perhaps even elements of string theory or other beyond-standardmodel physics.

Here's the updated plot with funnels added to each chimney. Each chim-ney now includes a gray cylinder and a brown funnel, representing the copies of $\operatorname{ds}^{2}(L)$, with labels indicating their positions in the sequence. The funnels extend from the bottom to the center of the chimneys.

Sure, let's make 5 separate copies of the equation for $\mathrm{ds}^{2}(\mathrm{~L})$. Each copy will be denoted with a subscript for clarity.

Given the equation:

$$
d s^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}
$$

We will create 5 copies, labelled $d s_{1}^{2}(L), d s_{2}^{2}(L), d s_{3}^{2}(L), d s_{4}^{2}(L)$, and $d s_{5}^{2}(L)$

## 1. First copy

$$
d s_{1}^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}
$$

2. Second copy:

$$
d s_{2}^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}
$$

3. Third copy:
$d s_{3}^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}$
4. Fourth copy:
$d s_{4}^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}$
5. Fifth copy:
$d s_{5}^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}$

Each of these copies represents the same equation, just labeled differently to indicate they are separate instances of $d s^{2}(L)$.

The image provided appears to be a plot showing the convergence of the Newton-Raphson method for finding the roots of two functions: $1-\rho^{2}$ and $\rho^{2}-1$. The plot includes markers indicating the roots of these equations. Here's a breakdown of what the plot represents:

1) Functions Plotted: The blue curve represents the function 1- $\rho^{2}$. The orange curve represents the function $\rho^{2}-1$.
2) Roots of the Functions: The red dots indicate the roots of the equation $1-\rho^{2}=0$, which occur at $\rho= \pm 1$. - The blue dots indicate the roots of the equation $\rho^{2}-1=0$, which also occur at $\rho= \pm 1$.
3) Newton-Raphson Iterations: The plot shows iterations of the Newton-Raphson method converging to these roots, with markers indicating the steps taken in the iterative process.
4) Plot Features: The $x$-axis represents the variable $\rho$. The $y$-axis represents the function values. - The title "Convergence of Newton-Raphson Method with Tachyonic Antitelephone"

Taking a more time-oriented approach to the nature of motion involves shift-ing focus from the spatial dimensions of motion (position, distance, velocity) to the temporal aspects (time elapsed, acceleration, rate of change). Here are some ways to do that:

1) Velocity-Time Graphs: Instead of relying solely on position-time graphs to understand motion, you can use velocity-time graphs. These graphs plot velocity against time, offering insights into how speed changes over time, which can be crucial for understanding acceleration and deceleration.
2) Acceleration: Emphasize the concept of acceleration, which measures the rate of change of velocity over time. By analyzing how acceleration varies with time, you gain a deeper understanding of how objects speed up or slow down.
3) Kinematic Equations: Use kinematic equations that involve time as a variable. These equations relate displacement, initial velocity, final velocity, acceleration, and time, providing a time-centric perspective on motion problem-solving.
4) Motion in Different Reference Frames: Consider motion from the perspective of different reference frames moving relative to each other over time. This approach can be especially useful in understanding concepts like relative velocity and inertial frames of reference.
5) Dynamic Systems Analysis: Analyze dynamic systems by considering how they evolve over time. This approach involves studying how various factors, such as forces and initial conditions, influence the motion of objects as time progresses.
6) Time-dependent Forces: Explore how forces acting on objects change over time. For example, in oscillatory motion, such as a simple harmonic oscil-lator, forces like spring force or gravitational force vary with time, leading to periodic motion.
7) Event-Based Analysis: Focus on specific events or milestones in the motion of an object and analyze how these events unfold over time. This ap-proach can help in understanding complex motions by breaking them down into smaller, time-bound segments.

By adopting a more time-oriented approach to motion, you can deepen your understanding of dynamic systems and phenomena, which is crucial in various fields such as physics, engineering, and even biology. This perspective enables a more nuanced analysis of motion beyond traditional spatial considerations.

The Gott Time Machine Equation is a theoretical concept proposed by physi-cist J. Richard Gott, which explores the possibility of time travel using cosmic strings. The equation relates the parameters of a cosmic string to the potential for closed timelike curves (CTCs) and hence the possibility of time travel.

One version of the Gott Time Machine Equation is given as:

$$
T=2 \pi \sqrt{\frac{R^{3}}{2 G \mu}}
$$

Where: - $T$ is the time duration required for a cosmic string to make a closed timelike curve. $-R$ is the radius of the circle around the cosmic string where the time machine is formed. $-G$ is the gravitational constant. - $\mu$ is the linear mass density of the cosmic string.

Another version of the equation involves the velocity v of the cosmic string:

$$
v=\frac{2 \pi G \mu}{c^{2}}
$$

Where: - $v$ is the velocity of the cosmic string. - $c$ is the speed of light.

These equations provide insight into the relationship between the parameters of a cosmic string and the potential for time travel. By manipulating these equations, one can explore various scenarios related to time travel using cosmic strings.

## Warp Drive

The Gott Time Machine Equation, proposed by physicist J. Richard Gott, is a theoretical equation derived from the theory of general relativity. This equation provides a mathematical framework for the potential construction of a time machine using cosmic strings.

Another form of the Gott Time Equation is:

$$
T=\int_{0}^{R} \frac{\sqrt{1-\frac{v^{2}}{c^{2}}}}{v} d v
$$

Where: - $T$ represents the time travel duration. $-R$ is the radius of the cosmic string loop. $-v$ is the velocity of the observer relative to the cosmic string loop. - $c$ is the speed of light in a vacuum.

This equation suggests that if an observer travels around a closed loop of cosmic string at a certain velocity, they could potentially experience time travel. However, it's worth noting that the feasibility and practicality of constructing such a time machine remain highly speculative and are subject to many unre-solved theoretical and practical challenges.

The concept of a warp drive, popularized by science fiction and explored in theoretical physics, involves the manipulation of spacetime to achieve faster-than-light travel. One of the proposed theoretical frameworks for a warp drive is the Alcubierre drive, named after physicist Miguel Alcubierre, who proposed it in 1994. The Alcubierre metric describes how spacetime can be "warped" to achieve apparent faster-than-light travel without violating the laws of relativity.

The key equation associated with the Alcubierre warp drive is the Alcubierre metric itself:

$$
d s^{2}=-\left(1-\frac{v^{2}}{c^{2}}\right) d t^{2}+2 \frac{v}{c} d x d t+d x^{2}+d y^{2}+d z^{2}
$$

Where: $-d s$ represents an infinitesimal interval of spacetime. $-d t$ is the infinitesimal time interval. $-d x, d y, d z$ are the infinitesimal spatial intervals in the $\mathrm{x}, \mathrm{y}$, and z directions respectively. $-v$ is the velocity of the "warp bubble" relative to the stationary observers. $-c$ is the speed of light in a vacuum.

In this equation, the term $1-\frac{v^{2}}{c^{2}} d t^{2}$ effectively describes the warping of spacetime, allowing for the apparent compression of space in front of the spaceship and expansion behind it. This warping creates a "bubble" of distorted spacetime, within which the spaceship can travel at velocities greater than the speed of light relative to distant observers.

It's important to note that while the Alcubierre metric provides a mathemat-ical solution consistent with general relativity, there are significant theoretical and practical challenges associated with the actual construction and operation of a warp drive, including the requirement for exotic matter with negative en-ergy density, which has yet to be observed. Therefore, the Alcubierre drive remains purely speculative at this point.

While both the Gott time machine equation and the Alcubierre metric are related to the manipulation of spacetime, they represent different concepts and mathematical formulations. Equating them directly wouldn't make physical sense, as they describe different phenomena. However, I can provide a compar-ison between the two:

## 1) Gott Time Machine Equation:

$$
T=\int_{0}^{R} \frac{\sqrt{1-\frac{v^{2}}{c^{2}}}}{v} d v
$$

This equation describes the time experienced by an observer traveling around a closed loop of cosmic string at a certain velocity. It's related to the concept of closed timelike curves and potential time travel scenarios.
2) Alcubierre Metric:

$$
d s^{2}=-\left(1-\frac{v^{2}}{c^{2}}\right) d t^{2}+2 \frac{v}{c} d x d t+d x^{2}+d y^{2}+d z^{2}
$$

This metric describes the distortion of spacetime around a spaceship, al-lowing for apparent faster-than-light travel by contracting space in front of the spaceship and expanding it behind.

While both involve the manipulation of spacetime, they have different im-plications and applications. The Gott time machine equation deals with the theoretical possibility of time travel using cosmic strings, while the Alcubierre metric explores the theoretical framework for a warp drive that could enable faster-than-light travel without violating the laws of physics.

Gott Time Machine Equation:

$$
T=\int_{0}^{R} \frac{\sqrt{1-\frac{v^{2}}{c^{2}}}}{v} d v
$$

Alcubierre Metric

$$
d s^{2}=-\left(1-\frac{v^{2}}{c^{2}}\right) d t^{2}+2 \frac{v}{c} d x d t+d x^{2}+d y^{2}+d z^{2}
$$

To equate them, we would need to find some way to relate the variables in the two equations. One possible approach could be to equate the integrand of the Gott Time Machine Equation to the time component of the Alcubierre Metric, although this is purely speculative and may not yield any meaningful result. Let's try:

This equation, however, doesn't appear to offer any straightforward solution and doesn't seem to have a direct physical interpretation. It's important to note that just because we can equate mathematical expressions doesn't mean they correspond to physical reality. In this case, attempting to equate these two equations doesn't seem to lead to any meaningful insights due to their fundamental differences in describing different physical phenomena.

To solve for c , we would first need to isolate it within the equation result-ing from the equating of the Gott Time Machine Equation and the Alcubierre Metric. However, given the complexity and lack of direct relationship between the two equations, it's unlikely that we'll find a straightforward solution for c .

Let's attempt to isolate c in the equation we formed earlier:

$$
\frac{\sqrt{1-\frac{v^{2}}{c^{2}}}}{v}=-\left(1-\frac{v^{2}}{c^{2}}\right) d t^{2}
$$

Rearranging terms and isolating c :

$$
\begin{gathered}
\sqrt{1-\frac{v^{2}}{c^{2}}}=-v\left(1-\frac{v^{2}}{c^{2}}\right) d t^{2} \\
1-\frac{v^{2}}{c^{2}}=v^{2}\left(1-\frac{v^{2}}{c^{2}}\right)^{2} d t^{4} \\
1-\frac{v^{2}}{c^{2}}=v^{2}\left(1-2 \frac{v^{2}}{c^{2}}+\frac{v^{4}}{c^{4}}\right) d t^{4} \\
1-\frac{v^{2}}{c^{2}}=v^{2}-2 v^{4} \frac{1}{c^{2}}+v^{6} \frac{1}{c^{4}} d t^{4} \\
1=\frac{v^{2}}{c^{2}}+v^{2}-2 v^{4} \frac{1}{c^{2}}+v^{6} \frac{1}{c^{4}} d t^{4} \\
1=\frac{v^{2}}{c^{2}}\left(1-2 v^{2}\right)+v^{6} \frac{1}{c^{4}} d t^{4} \\
\frac{v^{2}}{c^{2}}\left(1-2 v^{2}\right)=1-v^{6} \frac{1}{c^{4}} d t^{4} \\
c^{2}=\frac{v^{2}}{\left(1-2 v^{2}\right)} \cdot \frac{1}{\left(1-v^{6} \frac{1}{c^{4}} d t^{4}\right)} \\
c^{2}=\frac{v^{2}}{1-2 v^{2}-v^{6} \frac{1}{c^{4}} d t^{4}}
\end{gathered}
$$

$$
\begin{gathered}
c^{2}\left(1-2 v^{2}-v^{6} \frac{1}{c^{4}} d t^{4}\right)=v^{2} \\
c^{2}-2 v^{2} c^{2}-v^{6} d t^{4}=v^{2} c^{4} \\
c^{2}\left(1-v^{6} d t^{4}\right)=2 v^{2} c^{2} \\
c^{2}=\frac{2 v^{2} c^{2}}{1-v^{6} d t^{4}} \\
c^{4}=\frac{2 v^{2} c^{2}}{1-v^{6} d t^{4}} \\
c^{4}\left(1-v^{6} d t^{4}\right)=2 v^{2} c^{2} \\
c^{4}-v^{6} d t^{4} c^{4}=2 v^{2} c^{2} \\
c^{4}\left(1-v^{6} d t^{4}\right)=2 v^{2} c^{2} \\
c^{2}=\frac{2 v^{2} c^{2}}{1-v^{6} d t^{4}}
\end{gathered}
$$

This manipulation didn't lead to a direct solution for c . It's possible that the original equation formed by equating the two expressions may not be solvable for $c$ in $a$ straightforward manner, or that there may be an error in the manipulation.

We can substitute $c^{2}$ from the obtained equation into $\mathrm{E}=$ $\mathrm{mc}^{2}$.

From the equation:

$$
\begin{gathered}
c^{2}=\frac{2 v^{2} c^{2}}{1-v^{6} d t^{4}} \\
c^{4}\left(1-v^{6} d t^{4}\right)=2 v^{2} c^{2} \\
c^{4}-v^{6} d t^{4} c^{4}=2 v^{2} c^{2} \\
c^{4}\left(1-v^{6} d t^{4}\right)=2 v^{2} c^{2} \\
c^{2}=\frac{2 v^{2} c^{2}}{1-v^{6} d t^{4}}
\end{gathered}
$$

Let's solve this equation for $c^{2}$ :

$$
\begin{gathered}
c^{2}\left(1-v^{6} d t^{4}\right)=2 v^{2} c^{2} \\
1-v^{6} d t^{4}=2 v^{2} \\
c^{2}=\frac{2 v^{2}}{1-v^{6} d t^{4}}
\end{gathered}
$$

Now, we can replace $\mathrm{c}^{2}$ in $E=m c^{2}$ with this expression:

$$
E=m\left(\frac{2 v^{2}}{1-v^{6} d t^{4}}\right)
$$

However, this expression for energy is not directly equivalent to $E=m c^{2}$ anymore. It shows that the energy depends on the velocity v and other factors introduced by the equation derived from the equating process, indicating a more complex relationship between energy, mass, velocity, and time in this hypothetical scenario.

Let's multiply $m$ with the expression inside the brackets:

$$
E=m\left(\frac{2 v^{2}}{1-v^{6} d t^{4}}\right)
$$

$$
E=\frac{2 m v^{2}}{1-v^{6} d t^{4}}
$$

Now the expression represents the energy E in terms of mass m , velocity v , and the factors introduced by the equation derived from the equating process.

To relate the expression for energy we obtained to the Alcubierre Metric, we need to consider the physical interpretation of each term in the equation.

The Alcubierre Metric describes the spacetime geometry around a hypothet-ical warp bubble, which allows for apparent faster-than-light travel. The energy required for such a warp drive is a complex topic and depends on various factors, including the properties of the exotic matter that would be needed to create and maintain the warp bubble.

In our derived expression for energy:

$$
E=\frac{2 m v^{2}}{1-v^{6} d t^{4}}
$$

The mass $m$ represents the mass of the object or spacecraft. The term $v$ represents the velocity of the spacecraft, and $d t$ represents the time interval.

In the context of the Alcubierre Metric, the energy required for the warp drive would likely involve factors related to the energy density of the exotic matter needed to warp spacetime. The equation we derived doesn't directly correspond to the energy requirements of the Alcubierre Metric, as it doesn't include terms related to the energy density of the warp bubble's "engine" or the curvature of spacetime induced by it.

Therefore, while we can manipulate equations mathematically, directly relat-ing our derived expression to the energy requirements of the Alcubierre Metric might not be straightforward or physically meaningful without additional con-siderations and assumptions about the nature of the warp drive technology.

Integrating the expression for energy could provide insight into the total energy required over a given period, but it's important to note that without a specific model for the energy density of the warp bubble's "engine" or the curvature of spacetime induced by it, the integration may not yield physically meaningful results. However, we can still perform the integration as an exercise:

$$
E=\frac{2 m v^{2}}{1-v^{6} d t^{4}}
$$

Integrating this expression with respect to time t over a given period $\Delta t$ :

$$
\int E d t=\int \frac{2 m v^{2}}{1-v^{6} d t^{4}} d t
$$

This integral would depend on the limits of integration and the specific func-tion for $\mathrm{v}(\mathrm{t})$, which would describe how the velocity of the spacecraft changes over time. However, integrating over a variable $t$ within the denominator intro-
duces complexities, especially with the presence of $v(t)$ and dt terms.

Without a specific model for $\mathrm{v}(\mathrm{t})$ or additional information about the cur-vature of spacetime induced by the warp bubble, it's challenging to provide a meaningful analytical solution. In practice, determining the energy require-ments for an Alcubierre warp drive would likely involve more sophisticated the-oretical and computational approaches, potentially requiring advanced concepts from theoretical physics and numerical simulations.

To continue, let's make a simplifying assumption that the velocity v is con-stant over the period of integration $\Delta \mathrm{t}$. With this assumption, we can take v outside the integral:

$$
\begin{gathered}
\int E d t=\int \frac{2 m v^{2}}{1-v^{6} d t^{4}} d t \\
=\frac{2 m v^{2}}{v^{6}} \int \frac{1}{1-\left(v^{6} d t^{4}\right)} d t \\
=\frac{2 m}{v^{4}} \int \frac{1}{1-u^{2}} d u
\end{gathered}
$$

where $u=v^{3} d t^{2}$
Now, we can integrate the expression $\frac{1}{1-u^{2}}$ with respect to $u$

$$
\int \frac{1}{1-u^{2}} d u=\frac{1}{2} \ln \left|\frac{1+u}{1-u}\right|+C
$$

Plugging this back into the previous expression:

$$
\begin{aligned}
& \frac{2 m}{v^{4}}\left(\frac{1}{2} \ln \left|\frac{1+u}{1-u}\right|\right)+C \\
& \quad=\frac{m}{v^{4}} \ln \left|\frac{1+u}{1-u}\right|+C^{\prime}
\end{aligned}
$$

Now, substituting back $u=v^{3} d t^{2}$

$$
=\frac{m}{v} \ln \left|\frac{1+v^{3} d t^{2}}{1-v^{3} d t^{2}}\right|+C^{\prime}
$$

This result represents the indefinite integral of the expression for energy over the time interval $\Delta t$. However, to find the total energy over the interval, we need to specify the limits of integration and then evaluate the integral accordingly.

Additionally, to make this analysis more physically meaningful, we would need to incorporate a model for how the velocity $v$ changes over time, as well as considerations for the energy density of the warp bubble's "engine" and the curvature of spacetime induced by it.

Let's continue by assuming a constant velocity $v$ over the integration interval $\Delta t$. We'll integrate the expression from $t_{0}$ to $t_{1}$ :

$$
\int_{t_{0}}^{t_{1}} E d t=\frac{m}{v} \int_{t_{0}}^{t_{1}} \ln \left|\frac{1+v^{3} d t^{2}}{1-v^{3} d t^{2}}\right| d t
$$

To solve this integral, we need to find the antiderivative of $\ln$ $\left\lvert\, \frac{1+v^{3} d t^{2}}{1-v^{3} d t^{2}}\right.$. $\mid$ We will denote $u=\frac{1++v^{3} d t^{2}}{1-v^{3} d t^{2}}$ and use the fact that $\frac{d u}{d t}=\frac{6 v^{3}}{\left(1-v^{3} d t^{2}\right)^{2}}$. Then:
$\int \ln |u| d u=u \ln |u|-u+C$

$$
\begin{gathered}
\int_{t_{0}}^{t_{1}} E d t=\frac{m}{v}\left[\frac{1+v^{3} d t^{2}}{1-v^{3} d t^{2}} \ln \left|\frac{1+v^{3} d t^{2}}{1-v^{3} d t^{2}}\right|-\frac{1+v^{3} d t^{2}}{1-v^{3} d t^{2}}\right]_{t_{0}}^{t_{1}} \\
=\frac{m}{v}\left[\frac{1+v^{3} d t_{1}^{2}}{1-v^{3} d t_{1}^{2}} \ln \left|\frac{1+v^{3} d t_{1}^{2}}{1-v^{3} d t_{1}^{2}}\right|-\frac{1+v^{3} d t_{1}^{2}}{1-v^{3} d t_{1}^{2}}-\frac{1+v^{3} d t_{0}^{2}}{1-v^{3} d t_{0}^{2}} \ln \left|\frac{1+v^{3} d t_{0}^{2}}{1-v^{3} d t_{0}^{2}}\right|+\frac{1+v^{3} d t_{0}^{2}}{1-v^{3} d t_{0}^{2}}\right]
\end{gathered}
$$

This expression represents the total energy required over the time interval $\left[t_{0}, t_{1}\right]$ for a spacecraft with a constant velocity $v$. To evaluate it further, we need specific values for $\mathrm{t}_{0}, \mathrm{t}_{1}, v$, and potentially other parameters.

To make progress, we need to introduce some values or assumptions for the energy density of the warp bubble's "engine" and the curvature of spacetime induced by it. However, it's important to note that these values are highly speculative and theoretical, as the concept of an Alcubierre warp drive is purely hypothetical and not supported by current scientific understanding.

For the energy density of the warp bubble's "engine," we could use a theo-retical value based on speculative physics concepts. Let's denote this as $\rho$.

For the curvature of spacetime induced by the warp bubble, we could use a theoretical value for the spacetime metric $\mathrm{g}_{\mu v}$, which would describe the curva-ture of spacetime within the bubble. Let's denote this as $\mathrm{g}_{\mu v}$.

However, without concrete theoretical models or experimental evidence, it's challenging to assign specific values to these parameters. Theoretical studies on the Alcubierre warp drive have proposed various values and assumptions, but they remain highly speculative and subject to significant uncertainties.

If you have specific values or assumptions in mind, or if you'd like to explore hypothetical scenarios further, please let me know, and I can incorporate them into the analysis.

Let's continue by incorporating the energy density $\rho$ of the warp bubble's "engine" and the curvature of spacetime $g_{\mu \nu}$ into our analysis.

First, we'll represent the energy density $\rho$ as the energy per unit volume within the warp bubble. This energy density would contribute to the total energy required for the warp drive operation.

Next, the curvature of spacetime induced by the warp bubble can be de-scribed by the Alcubierre Metric. This metric, which we denoted as $d s^{2}$, de-scribes the spacetime geometry around the warp bubble. The specific values or functions of $g_{\mu \nu}$ would depend on the details of the warp bubble's geometry and the distribution of energy within it.

We could express the total energy E required for the warp drive operation as the sum of the energy associated with the spacecraft's motion and the en-ergy associated with the curvature of spacetime induced by the warp bubble's "engine."

$$
\begin{gathered}
E_{\text {total }}=E_{\text {kinetic }}+E_{\text {curvature }} \\
E_{\text {total }}=\frac{1}{2} m v^{2}+\rho \cdot \text { Volume }
\end{gathered}
$$

Here, $E_{\text {kinetic }}$ represents the kinetic energy of the spacecraft, $\rho$. Volume represents the energy associated with the curvature of spacetime induced by the warp bubble's "engine", where Volume is the volume of the warp bubble.

The energy density $\rho$ and the curvature of spacetime $g_{\mu \nu}$ would determine the energy required for the warp drive operation. However, without specific values or models for these parameters, we cannot provide numerical calculations or further analysis.

To isolate and solve for v in the equation provided, we need to rearrange terms and apply appropriate mathematical operations. Let's start by rewriting the equation:

$$
E_{\text {total }}=\frac{1}{2} m v^{2}+\rho \cdot \text { Volume }
$$

Subtracting $\rho$. Volume from both sides:

$$
\frac{1}{2} m v^{2}=E_{\text {total }}-\rho \cdot \text { Volume }
$$

To isolate $v^{2}$, we multiply both sides by $\frac{2}{m}$ :

$$
v^{2}=\frac{2}{m}\left(E_{\text {total }}-\rho . \text { Volume }\right)
$$

Finally, to solve for $v$, we take the square root of both sides:

$$
\left.v=\sqrt{\frac{2}{m}}\left(E_{\text {total }}-\rho . \text { Volume }\right)\right)
$$

This equation gives the velocity v of the spacecraft required for the warp drive operation, given the total energy $\mathrm{E}_{\text {total }}$, the mass $m$ of the spacecraft, and the energy density $\rho$ of the warp bubble's "engine". The volume term represents the volume of the warp bubble.

It's important to note that obtaining actual numerical values for $v$ would require specific values for $E_{\text {total }}, m, \rho$, and the volume of the warp bubble. Additionally, this equation assumes a simplified model and may not capture all the complexities involved in warp drive technology.

## Isolating ds4

The super equation derived earlier encompasses gravitational, quantum mechan-ical, and Hawking radiation effects:

$$
F(\rho)=\theta+b(L)-d(L)+d s^{2}(L)+r(\phi(L))+\frac{\partial \Psi}{\partial t}(L)-\nabla^{2} \Psi(L)+V(x, y)-|\Psi(x, y)|^{2}
$$

where: $\rho$ : Generalized parameter.
$\theta$ : Angular parameter.
$b(L)$ : Function related to a specific length scale L.
$\mathrm{d}(\mathrm{L})$ : Another length-dependent function.
$\mathrm{Ds}^{2}(\mathrm{~L})$ : Differential element squared.
$r(\phi(\mathrm{~L}))$ : Radial function dependent on angle $\phi$.
$\frac{{ }_{\partial} \Psi}{\partial t}(\mathrm{~L}):$ Time derivative of the wave function $\Psi$.

$$
d s^{2}(L)=F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}
$$

## Achieving ds4

To achieve $d s^{4}(L)$ from the isolated equation for $d s^{2}(L)$, we directly square both sides:

$$
\left(d s^{2}(L)\right)^{2}=\left(F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}\right)^{2}
$$

Thus, the equation for $d s^{4}(L)$ is:
$d s^{4}(L)=\left(F(\rho)-\theta-b(L)+d(L)-r(\phi(L))-\frac{\partial \Psi}{\partial t}(L)+\nabla^{2} \Psi(L)-V(x, y)+|\Psi(x, y)|^{2}\right)^{2}$

## Graphs

This section presents a selected set of graphs to depict the correlations between ds 4 , gravity, qm , and hr .


Figure 1: Convergence of Newton-Raphson Method at 1-rho


Figure 2: Antitachyonic Gene Expression Time duration for different values of $R$ and mu


Figure 3: QM, GR Transmission Lines


Figure 4: Q-Thrust Magnitudal


Figure 5: Gravity Microprocessor


Figure 6: Gott Time


Figure 7: Enter Caption


Figure 8: Direction of Time


Figure 9: Presence of Closed Timelike Curves
Perturbation of a Closed Timelike Curve (CTC)


Figure 10: Perturbed Closed Timelike Curves


Figure 11: DS2

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Figure 12: Closed Timelike Curve Qubit Encapsulation

## Code

This section presents code snippets encoding DS4.
import numpy as np
import matplotlib.pyplot as plt
\# Define the functional forms coefficients
a1, a2, a3, a4, a5, a6, a7, a8 = 1, 2, 3, 4, 5, 6, 7, 8 \# Example
coefficients
\# Define the bounds for $L$
L_min $=0$
L_max $=10$
\#Define the equation for $\mathrm{ds}^{\wedge} 4(\mathrm{~L})$
def ds4_equation(L):
\# Functional forms
b_L $=\mathrm{a} 1 * \mathrm{~L}^{* *} 2+\mathrm{a} 2 * \mathrm{~L}+\mathrm{a} 3$
$\mathrm{d} \_\mathrm{L}=\mathrm{a} 4 * \mathrm{np} \cdot \sin (\mathrm{L})+\mathrm{a} 5 * \mathrm{np} \cdot \cos (\mathrm{L})$
phi_L = np.pi / 2 \# Example value for simplicity
r_phi_L $=$ a6 * phi_L $* * 2+a 7 *$ phi_L + a8
\# Compute $\mathrm{ds}^{\wedge} 4$ (L)

return ds4_L
\# Generate L values over the interval [L_min, L_max]
L_values $=$ np.linspace $\left(L_{-} \min , L_{-} \max , 100\right)$
ds4_values = ds4_equation(L_values)
\# Plot the function $\mathrm{ds}^{\wedge} 4(\mathrm{~L})$
plt.figure $($ figsize $=(10,6))$
plt.plot(L_values, ds4_values, label=r'\$ds^4(L)\$', color='blue')
plt.xlabel('L')
plt.ylabel(r'\$ds^4(L)\$')
plt.title('Function \$ds^4(L)\$ over the interval [\$L_\{
\$L_\{ $\left.\backslash m a t h r m\{\max \}\} \$]^{\prime}\right)$
plt.axhline( 0 , color='black', linewidth $=0.5$, linestyle='--')
plt.grid(True)
plt.legend()
plt.show()
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.animation import FuncAnimation
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\# Function to compute $\mathrm{ds}^{\wedge} 4(\mathrm{~L})$
def compute_ds4(rho_values, F_rho, theta, b_L, d_L, r_phi_L, d_Psi_dt_L, nabla2_Psi_L, V_x_y, Psi_x_y):
ds4 $=($ np.abs(F_rho $/$ rho_values $) * * 2+$
np.abs(theta / rho_values)**2 +
np.abs(b_L / rho_values)**2 +
np.abs(d_L / rho_values)**2 +
np.abs(r_phi_L / rho_values)**2 +
np.abs(d_Psi_dt_L / rho_values)**2 +
np.abs(nabla2_Psi_L / rho_values)**2 +
np.abs(V_x_y / rho_values)**2 +
np.abs(np.abs(Psi_x_y)**2 / rho_values) ${ }^{* *} 2$ )
return ds 4
\# Function to compute $\mathrm{X}(\mathrm{L})$
def compute_X(rho_values, F_rho, theta, b_L, d_L, r_phi_L, d_Psi_dt_L, nabla2_Psi_L, V_x_y, Psi_x_y):
$\mathrm{X}=\left(\left(\mathrm{np} . \mathrm{abs}\left(\mathrm{F} \_ \text {rho } / \text { rho_values }\right)^{* *} 2\right) *(1-\text { rho_values })^{* *} 2+(\mathrm{np} . \mathrm{abs}(\right.$ theta $/$ rho_values $) * * 2) *(1-$ rho_values $) * * 2+\left(\mathrm{np} . \mathrm{abs}\left(\mathrm{b} \_\mathrm{L} /\right.\right.$
rho_values $\left.)^{* *} 2\right) *(1-$ rho_values $) * * 2+\left(\mathrm{np.abs}\left(\mathrm{~d} \_\mathrm{L} /\right.\right.$ rho_values $\left.) * * 2\right) *(1-$ rho_values $) * * 2+\left(\mathrm{np} . \mathrm{abs}\left(\mathrm{r} \_\mathrm{phi}\right.\right.$ _L / rho_values $\left.) * * 2\right) *(1-$ rho_values $) * * 2+\left(\right.$ np.abs $\left(\mathrm{d}_{-}\right.$Psi_dt_L / rho_values $\left.) * * 2\right) *(1-$ rho_values $) * * 2+($ np.abs $($ nabla2_Psi_L / rho_values $) * * 2) *(1-$

rho_values)**2)
return X
\# Define parameters for the equations
F_rho = np.random.rand() \# Random value for demonstration
theta $=$ np.random.rand () \# Random value for demonstration
b_L = np.random.rand() \# Random value for demonstration
d_L = np.random.rand() \# Random value for demonstration
r_phi_L = np.random.rand() \# Random value for demonstration
d_Psi_dt_L = np.random.rand() \# Random value for demonstration
nabla2_Psi_L = np.random.rand() \# Random value for demonstration
V_x_y = np.random.rand() \# Random value for demonstration
Psi_x_y $=$ np.random.rand ()$+1 \mathrm{j} *$ np.random.rand() \# Random value for demonstration
\# Create figure and axes
fig $=$ plt.figure $($ figsize $=(10,6))$
ax $=$ fig.add_subplot(111, projection='3d')
\# Set up lines
line_ds4, = ax.plot([], [], [], lw=2, label=' $\left.d s^{\wedge} 4(\mathrm{~L})^{\prime}\right)$
line_X, = ax.plot([], [], [], lw=2, label=' $\left.\mathrm{X}(\mathrm{L})^{\prime}\right)$
\# Set up labels and titles
ax.set_xlabel ('Time')
ax.set_ylabel('ds^4(L)') .
ax.set_zlabel(' $\left.\mathrm{X}(\mathrm{L})^{\prime}\right)$
ax.set_title('Animation of $d s^{\wedge} 4(\mathrm{~L})$ and $\mathrm{X}(\mathrm{L})$ with Newton-Raphson method')
\# Set up legend
ax.legend()
\# Initialization function: plot the background of each frame def init():
line_ds4.set_data([], [])
line_ds4.set_3d_properties([])
line_X.set_data([], [])
line_X.set_3d_properties([])
return line_ds4, line_X
time $=$ np.linspace $(0,1,100)$ \# Define time
\# Animation function: this is called sequentially def animate(i):
rho $=\mathrm{np} . \sin (2 * \mathrm{np} . \mathrm{pi} *$ time[i] $) / 2+0.5 \#$ Vary rho sinusoidally from 0 to 1 rho_values $=$ np.full_like(time, rho)

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ds4 = compute_ds4(rho_values, F_rho, theta, b_L, d_L, r_phi_L, d_Psi_dt_L, nabla2_Psi_L, V_x_y, Psi_x_y)
$X=$ compute_X(rho_values, F_rho, theta, b_L, d_L, r_phi_L, d_Psi_dt_L, nabla2_Psi_L, V_x_y, Psi_x_y)
line_ds4.set_data(time[:i], ds4[:i])
line_ds4.set_3d_properties(X[:i])
line_X.set_data(time[:i], X[:i])
line_X.set_3d_properties(ds4[:i])
\# Dynamically adjust z-axis limits
buffer $=0.1$ \# Buffer to ensure lines remain visible
\# Check if arrays are not empty before computing min and max
if ds4[:i].size $>0$ and $X[: i]$.size $>0$ :
$\min \_$value $=\min (n p \cdot \min (d s 4[: i])$, np.min $(X[: i]))$
$\max \_$value $=\max (\mathrm{np} \cdot \max (\mathrm{ds} 4[: i]), \operatorname{np} \cdot \max (X[: i]))$

```
else:
    min_value, max_value = 0,1 # Set default values if arrays are empty
    ax.set_zlim(min_value - buffer, max_value + buffer)
    return line_ds4, line_X
```

\# Call the animator
anim $=$ FuncAnimation(fig, animate, init_func=init, frames=len(time), interval=50, blit=True)
plt.show()

## Conclusivity

This document thoroughly combines General Relativity, Quantum Mechanics, and Hawking Radiation to produce the super equation - DS4. The expert ma-nipulation of this equation can lead to several innovations in a new era.

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