

Trying to Create Biquadratic Formula

Rishikesh Biswas

KVS

Email: rishikesh13611[at]gmail.com

Abstract: In this paper, we are going to see how I rewrote the quartic equation and tried to create a biquadratic formula by using the quadratic formula and as a result of an experiment, let's see what it can do. As the title suggests, that is "Trying to Recreate the Biquadratic Formula", I have tried to create a biquadratic formula in my calculation.

Keywords: Equation: A mathematical expression/statement with an equal to sign. Quartic/Biquadratic Equation: An equation with the highest degree of 4.

Cubic Equation: An equation with the highest degree of 3. **Quadratic Equation:** An equation with the highest power of 2. **Quadratic formula:** A formula that is used to find the variable x in any quadratic polynomial.

1. Introduction

In this paper, we are going to see how I rewrote the quartic equation and tried to create a [1] biquadratic formula by using the [2] quadratic formula and as a result of an experiment, let's see what it can do. As the title suggests, that is "Trying to Recreate the Biquadratic Formula", I have tried to create a biquadratic formula in my calculation.

We can use the formula in several situations but it was just my *experiment*.

2. Work

For first calculation variation; Having the constant 0.

$$x^2 \left(a \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)^2 + b \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right) \right) + \left(c \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right)^2 + d \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right) + e \right) = 0$$

$$x^2 \left(a \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)^2 + b \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right) \right) = - \left(c \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right)^2 + d \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right) + e \right)$$

$$x^2 = \frac{- \left(c \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right)^2 + d \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right) + e \right)}{a \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)^2 + b \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)}$$

$$x = \sqrt{\frac{- \left(c \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right)^2 + d \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right) + e \right)}{a \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)^2 + b \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)}}$$

$$x = \frac{\sqrt{- \left(c \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right)^2 + d \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right) + e \right)}}{\sqrt{a \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)^2 + b \left(\frac{-b \pm \sqrt{b^2 - 4af}}{2a} \right)}}$$

$$x = \frac{\sqrt{- \left(c \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right)^2 + d \left(\frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \right) + e \right)}}{\sqrt{a \left(\frac{-b \pm b}{2a} \right)^2 + b \left(\frac{-b \pm b}{2a} \right)}}$$

$$\text{Let } \frac{-d \pm \sqrt{d^2 - 4ce}}{2c} \text{ be } \frac{m}{n},$$

$$ax^4 + bx^3 + cx^2 + dx + e = 0$$

$$(ax^4 + bx^3) + (cx^2 + dx + e) = 0$$

$$X^2(ax^2 + bx) + (cx^2 + dx + e) = 0$$

Let f be a real number such that $f = 0$

$$x^2(ax^2 + bx + f) + (cx^2 + dx + e) = 0$$

Let's use the quadratic formula

$$x = \frac{\sqrt{- \left(c \left(\frac{m}{n} \right)^2 + d \left(\frac{m}{n} \right) + e \right)}}{\sqrt{a \left(\frac{y}{z} \right)^2 + b \left(\frac{y}{z} \right)}}$$

$$x = \frac{\sqrt{- \left(\frac{cm^2}{n^2} + \frac{dm}{n} + e \right)}}{\sqrt{\frac{ay^2}{z^2} + \frac{by}{z}}}$$

$$x = \frac{\sqrt{-1 \times \left(\frac{cm^2}{n^2} + \frac{dm}{n} + e \right)}}{\sqrt{\frac{ay^2}{z^2} + \frac{by}{z}}}$$

$$x = \frac{\sqrt{-1} \times \sqrt{\left(\frac{cm^2}{n^2} + \frac{dm}{n} + e \right)}}{\sqrt{\frac{ay^2}{z^2} + \frac{by}{z}}}$$

$$x = \frac{\sqrt{-1} \times \sqrt{\left(\frac{cm^2}{n^2} + \frac{dm}{n} + e \right)}}{\sqrt{\frac{ay^2}{z^2} + \frac{by}{z}}}$$

$$x = \frac{i\sqrt{\left(\frac{cm^2}{n} + \frac{dm}{n} + e\right)}}{\sqrt{\frac{ay^2}{z^2} + \frac{by}{z}}}$$

Now just put the values of m , n , y and z .

3. Conclusion

In summary, I have just tried to create the biquadratic formula using quadratic formulas.

References

- [1] Lodovico Ferrari is attributed with the discovery of the solution to the quartic in 1540
- [2] The quadratic formula was developed during the Islamic Golden Age, attributed to mathematicians such as al-Khwarizmi around the 9th century.

Author Profile

Rishikesh Biswas, a super ordinary 8th grader in India, who has contributed a little to the field of mathematics by doing nothing much by just publishing five research papers (excluding this one) and a book. Besides that, the author plays tabla (Indian Classical Musical Instrument) and has a national scholarship in it from the Ministry of Culture. Author has played chess in nationals as well.