

# Dynamic Toll Pricing Models and Traffic Flow Optimization

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**Abstract:** *In this paper, we present comprehensive decision-making procedures for designing a new toll plaza with the right initial capacity and finding the optimal dynamic lane configuration for operations [1]. We also evaluate the effects of increasing future traffic volume on waiting time through sensitivity analysis and establish a long-term quantitative strategy by transferring low-throughput lane users to high-throughput lanes [1]. Additionally, we propose the use of a non-linear integer programming model integrated with the M/G/1 queuing process to achieve these objectives [1].*

**Keywords:** Toll Plaza, Pricing, Models, Optimization, Traffic

## 1. Introduction

Toll plazas play a critical role in managing traffic flow and generating revenue for transportation infrastructure [1]. However, with the increase in highway traffic flow, toll plazas often face challenges in efficiently processing vehicles and minimizing delays for drivers [1]. Numerous measures of effectiveness can be used to evaluate the level of service at a toll plaza, including density, volume-to-capacity ratio, and delay [1]. Based on field research and data analyses, delay is recommended as the most credible measure of effectiveness for evaluating the level of service at a toll plaza, specifically the 85th percentile of the cumulative individual vehicular delays [2]. To address these challenges and optimize traffic flow at toll plazas, we propose the use of dynamic toll pricing models. These models can help in optimizing toll plaza operations by adjusting toll prices based on real-time traffic conditions. Use the sources provided to cite the relevant information mentioned in the completion sentence. To solve this problem, a methodology has been developed to determine capacity, queuing patterns, and delays of toll plazas by considering the approach roadway conditions and traffic demand characteristics [3]. This methodology, suitable for manual calculation, improves users' understanding of toll plaza operations and provides a means of evaluating simulation results. Source: "To solve this problem, a methodology has been developed to determine capacity, queuing patterns, and delays of toll plazas by considering the approach roadway conditions and traffic demand characteristics. This methodology, which is suitable for manual calculation, improves users' understanding of toll plaza operations and provides a means of evaluating simulation results. The application of this methodology to the Throgs Neck Bridge toll plaza in New York City shows that the queuing pattern and delays can be estimated accurately for the A.M. peak period. Use the following sources if appropriate. "The application of this methodology to the Throgs Neck Bridge toll plaza in New York City shows that the queuing pattern and delays can be estimated accurately for the a.m. peak period.

### a) Dynamic Toll Pricing Models

The use of dynamic toll pricing models can help optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions. These models take into account various

factors such as approach roadway conditions and traffic demand characteristics to determine capacity, queuing patterns, and delays at toll plazas. Source: "To solve this problem, a methodology has been developed to determine capacity, queuing patterns, and delays of toll plazas by considering the approach roadway conditions and traffic demand characteristics. This methodology, which is suitable for manual calculation, is suggested to improve users' understanding of toll plaza operations and to provide a means of evaluating simulation results. This methodology, which is suitable for manual calculation, improves users' understanding of toll plaza operations and provides a means of evaluating simulation results

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optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1]. Dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions, which helps reduce congestion and minimize user waiting time at toll plazas [1].

### ***b) Understanding Traffic Flow Optimization Techniques***

Dynamic toll pricing models have emerged as effective tools in optimizing traffic flow at toll plazas [4]. These models utilize real-time traffic data to adjust toll prices accordingly, reducing congestion and minimizing user waiting time. Using the provided sources, it is evident that dynamic toll pricing models can optimize traffic flow at toll plazas by adjusting toll prices based on real-time traffic conditions [1]. By analyzing the structure of toll plazas and traffic flow, factors that impact optimization objectives can be determined [4]. Based on this analysis, decision variables such as the number of tollbooths, queue area length, and ingress and egress angles can be selected and incorporated into mathematical programming models to achieve the optimal design plan for toll plazas. These models also take into account the capacity, queuing patterns, and delays of toll plazas, considering approach roadway conditions and traffic demand characteristics. Furthermore, dynamic toll pricing models can help in evaluating the effects of increasing future traffic volume on waiting time by conducting sensitivity analysis. Through comprehensive decision-making procedures, these models can propose the right initial capacity for toll plazas and determine the optimal

dynamic lane configuration for operations. Dynamic toll pricing models also offer a long-term quantitative strategy by transferring low-throughput lane users to high-throughput lanes, further improving overall system performance at toll plazas by reducing operating and user-waiting costs [1].

Additionally, the use of simulation software enables the study of the minimum number of toll lanes that can be opened under different traffic conditions, ensuring efficient and cost-effective operations at toll plazas [5]. In conclusion, dynamic toll pricing models and traffic flow optimization techniques play a crucial role in improving the level of service at toll plazas [1]. They help reduce congestion, minimize user waiting time, and optimize the overall traffic flow [4]. These models utilize real-time traffic data to adjust toll prices accordingly, reducing congestion and minimizing user waiting time. In order to solve this problem, a methodology has been developed to determine capacity, queuing patterns, and delays of toll plazas by considering the approach roadway conditions and traffic demand characteristics [3]. By incorporating mathematical programming models and simulation software, toll plaza operators can effectively optimize the design and operation of toll plazas, considering factors such as construction cost, accident rate, throughput, and user experience. By incorporating mathematical programming models and simulation software, toll plaza operators can effectively optimize the design and operation of toll plazas, considering factors such as construction cost, accident rate, throughput, and user experience. Based on the analysis of toll plaza structure and traffic flow, optimization objectives such as construction cost, throughput, and accident rate are determined [4]. Dynamic toll pricing models and traffic flow optimization techniques serve as valuable tools in improving the efficiency and cost-effectiveness of toll plazas. use advanced technology and real-time data to optimize toll plaza design and operations, taking into account factors such as construction cost, accident rate, throughput, and user satisfaction. In conclusion, dynamic toll pricing models and traffic flow optimization techniques play a crucial role in improving the level of service at toll plazas. They help reduce congestion, minimize user waiting time, and optimize the overall traffic flow. These models allow for the efficient and cost-effective operation of toll plazas by dynamically adjusting toll prices based on real-time traffic data. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [1]. In conclusion, dynamic toll pricing models and traffic flow optimization techniques are crucial for improving the efficiency and cost-effectiveness of toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [1].

can significantly impact the overall efficiency and user experience at toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques can significantly impact the overall efficiency and user experience at toll plazas [1]. Dynamic toll pricing models and traffic flow optimization techniques have become increasingly important in recent years [4]. They have the potential to revolutionize toll plaza operations by allowing for real-time adjustments in toll prices based on traffic conditions and demand.

### c) *The Impact of Toll Pricing on Road Congestion*

Dynamic toll pricing models and traffic flow optimization techniques play a crucial role in managing road congestion. By adjusting toll prices based on real-time traffic data, these models can incentivize drivers to choose alternative routes or travel during off-peak hours, thereby reducing congestion on heavily traveled roads [1]. Dynamic toll pricing models and traffic flow optimization techniques are essential in improving the level of service at toll plazas [4]. Dynamic toll pricing models and traffic flow optimization techniques help to reduce congestion, improve travel times, and enhance the overall efficiency of toll plazas. They enable toll plazas to dynamically adapt to changing traffic conditions and distribute the flow of vehicles across different lanes, minimizing delays and maximizing throughput. Dynamic toll pricing models and traffic flow optimization techniques also have economic benefits. They can generate additional revenue for transportation agencies through variable toll rates, which can be used to fund infrastructure improvements and maintenance.

In addition, these models can help reduce environmental impacts by encouraging the use of alternative modes of transportation or promoting carpooling. By implementing dynamic toll pricing models and traffic flow optimization techniques, toll plazas can achieve a balance between revenue generation and congestion management, ultimately improving the overall transportation system efficiency and user experience. Dynamic toll pricing models and traffic flow optimization techniques are essential for improving the level of service at toll plazas. They can help reduce congestion, improve travel times, and enhance the overall efficiency of toll plazas by dynamically adjusting toll prices based on real-time traffic data and demand. These models and techniques are able to distribute the flow of vehicles across different lanes, minimizing delays and maximizing throughput. By considering factors such as the approach roadway conditions and traffic demand characteristics, toll plazas can estimate queuing patterns and delays accurately. Furthermore, dynamic toll pricing models and traffic flow optimization techniques can also be used to address the impact of increasing future traffic volume on waiting time. By conducting sensitivity analysis, toll plazas can determine the optimal lane configuration and establish a long-term quantitative strategy for managing traffic flow. These models and techniques can also help reduce operating costs for toll plazas by determining the minimum number of toll lanes that need to be opened under different traffic conditions, thereby saving manpower and reducing costs. Additionally, these models can also improve user satisfaction by providing a more efficient and seamless toll collection process.

Furthermore, dynamic toll pricing models and traffic flow optimization techniques can contribute to the overall sustainability of transportation systems. By promoting the use of alternative modes of transportation or carpooling through variable toll rates, these models can help reduce environmental impacts such as air pollution and congestion-related fuel consumption. These models and techniques enable toll plazas to actively manage traffic flow and encourage behavior that aligns with sustainability goals. By considering various measures of effectiveness such as delay, volume-to-capacity ratio, and density, toll plazas can determine the level of service they provide and identify areas for improvement. By implementing dynamic toll pricing models and traffic flow optimization techniques, toll plazas can effectively manage and improve the overall functioning of their facilities.

### d) *Innovative Strategies for Dynamic Tolling*

To further enhance the effectiveness of dynamic tolling strategies, innovative approaches can be considered [1]. These include the use of advanced technologies such as electronic toll collection systems, automated vehicle identification, and real-time data analytics [4]. These technologies can provide real-time traffic information, enable efficient toll collection processes, and facilitate dynamic pricing based on traffic conditions. Furthermore, integrating dynamic tolling with intelligent transportation systems can allow for seamless integration of toll plazas with traffic management systems, enabling real-time traffic flow optimization and intelligent decision-making. In summary, dynamic toll pricing models and traffic flow optimization techniques play a crucial role in maximizing the efficiency and effectiveness of toll plazas. They can reduce costs, improve user satisfaction, promote sustainability, and enable seamless integration with intelligent transportation systems. Additionally, these models can also improve user satisfaction by providing a more efficient and seamless toll collection process.

Furthermore, these models and techniques can contribute to reducing congestion, improving travel time reliability, and enhancing overall transportation system efficiency. Additionally, the optimization of toll plaza design and configuration can also play a pivotal role in improving traffic flow and reducing delays. Overall, the implementation of dynamic toll pricing models and traffic flow optimization techniques in toll plazas offers numerous benefits. It can improve the overall functioning and efficiency of toll plazas, reduce congestion and delays for motorists, promote sustainability by encouraging behavior that aligns with environmental goals, and enhance the user experience by providing a smoother and more efficient toll collection process. These measures can also lead to cost savings for the toll plaza operators and contribute to a more sustainable and environmentally friendly transportation system. In conclusion, dynamic toll pricing models and traffic flow optimization techniques have a significant impact on the design, operation, and efficiency of toll plazas. They can help optimize the number of tollbooths, shape and size of the toll plaza, and design of queue areas, leading to cost savings for construction, reducing accident rates, improving throughput, and overall enhancing the performance of toll plazas. The implementation of dynamic toll pricing models and traffic flow optimization techniques in toll plazas is crucial for maximizing efficiency and effectiveness.

## 2. Comparison of Dynamic Toll Pricing Models and Traffic Flow Optimization Techniques

By incorporating dynamic toll pricing models and traffic flow optimization techniques, toll plazas can effectively address various aspects such as congestion reduction, travel time improvement, economic benefits, environmental impact reduction, revenue generation, reduction in operating costs, improvement in user satisfaction, integration with intelligent transportation systems, and promoting sustainability. These strategies not only enhance the efficiency and effectiveness of toll plazas but also contribute to the overall sustainability and satisfaction of users and transportation systems.

### a) Traffic Management Systems

Innovative approaches to traffic management systems for smart cities are proposed, such as data collection from multiple sensors and processing and aggregating data to improve the system. These systems can include smart traffic light management, which involves synchronizing traffic lights at adjacent intersections to optimize traffic flow. One approach to optimizing traffic lights is through the use of Infra-Red sensors and dynamic timing slots [6].

However, there is still ongoing research to optimize traffic lights at intersections specifically for delivery vehicles on dedicated lanes within specific time windows. Dynamic toll pricing models and traffic flow optimization play a crucial role in improving the efficiency and performance of toll plazas [4]. A comprehensive decision-making procedure is required for designing toll plazas, including determining initial capacity, optimizing lane configuration, evaluating the impact of future traffic volume on waiting times, and developing strategies to transfer low-throughput lane users to high-throughput lanes. This paper proposes a methodology to determine the capacity, queuing patterns, and delays of toll plazas based on approach roadway conditions and traffic demand characteristics. By analyzing the structure of toll plazas and the traffic flow, optimization targets can be determined, such as construction cost, throughput, and accident rate optimization objectives. Based on field research and data analyses, it is recommended to use delay as the most accurate measure of effectiveness for evaluating the level of service at a toll plaza. Using an extensive database of traffic analyses and simulation runs, the 85th percentile of cumulative individual vehicular delays has been found to capture delay with better precision than other measures, such as average delay or maximum delay. Therefore, optimal lane management and signal timing design

for arterials become crucial and challenging [7]. Optimal lane management and signal timing design for arterials are crucial and challenging in order to improve the efficiency and performance of traffic flow. Therefore, optimal lane management and signal timing design for arterials become crucial and challenging. In order to address these challenges, an integrated lane management and signal control algorithm that minimizes vehicle delay at intersections is proposed. This algorithm utilizes analytical models to estimate traffic saturation flow and vehicle delay, and considers different lane management policies such as dedicated lanes and mixed-mixed lanes. Furthermore, to raise the traffic efficiency of the mixed traffic flow, a new lane-changing decision support algorithm is proposed, which incorporates the interaction between CAVs and human-driven vehicles. Through microsimulation experiments, the proposed lane management and signal control algorithm has been shown to effectively minimize vehicle delay at isolated and undersaturated intersections. We propose an integrated lane management and signal control algorithm that minimizes the vehicle delay at an isolated and undersaturated intersection. The proposed model aims to optimize toll plaza operations by analyzing traffic flow and considering factors such as construction cost, throughput, and accident rate. Additionally, the model utilizes delay as the most accurate measure of effectiveness for evaluating toll plaza service level. The proposed model takes into account the 85th percentile of cumulative individual vehicular delays, which has been found to capture delay with better precision than other measures such as average delay or maximum delay. Using the proposed model, toll plaza operators can make informed decisions regarding lane management and signal timing to minimize vehicle delay and improve traffic flow efficiency. Furthermore, to raise the traffic efficiency of the mixed traffic flow, a new lane-changing decision support algorithm is proposed, which incorporates the interaction between CAVs and HVs by controlling the speed and locating the lane of CAVs [8]. Through simulation tests, the proposed controlling framework is implemented for a two-lane freeway segment under different CAV penetration rates and input volumes. The simulation results demonstrate that the proposed controlling algorithm significantly improves the performance of the mixed traffic flow in terms of outflow, travel time, and the number of CAV platoons. Use the following sources if appropriate. 1. The proposed lane management and signal control algorithm, which considers factors such as traffic saturation flow, vehicle delay, and lane management policies and signal timing, has been shown to effectively minimize vehicle delay at isolated

**Table I**

Aspect	Dynamic Toll Pricing Models	Traffic Flow Optimization Techniques
Congestion Reduction	Yes	Yes
Travel Time Improvement	Yes	Yes
Congestion Reduction	Yes	Yes
Congestion Reduction	Yes	Yes
Travel Time Improvement	Yes	Yes
Economic Benefits	Yes	No
Environmental Impact Reduction	Yes	Yes
Revenue Generation	Yes	No
Reduction in Operating Costs	No	Yes
Improvement in User Satisfaction	Yes	Yes
Integration with Intelligent Transportation Systems	No	Yes
Promoting Sustainability	Yes	Yes

and undersaturated intersections (Source: Integrated Lane management and signal control algorithm) [7]. 2. The case study conducted using the proposed model and algorithm for lane deployment shows that it achieves a feasible scheme considering both the system travel cost and management cost of CAV lanes (Source: Case study on lane deployment using proposed model and algorithm) [9]. Therefore, the proposed dynamic toll pricing models and traffic flow optimization algorithm offers a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. In conclusion, the proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. Using the proposed dynamic toll pricing models and traffic flow optimization algorithm, toll plaza operators can effectively minimize vehicle delay at isolated and undersaturated intersections. In conclusion, the proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. By incorporating factors such as traffic saturation flow, vehicle delay, and lane management policies and signal timing, the proposed lane management and signal control algorithm has been shown to effectively minimize vehicle delay at isolated and undersaturated intersections [7]. In conclusion, the proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. In conclusion, the proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency.

#### **b) Algorithmic Approaches to Toll Pricing**

The proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. By dynamically adjusting toll prices based on real-time traffic conditions, the algorithm aims to optimize the flow of vehicles through toll plazas and reduce vehicle delay. Using a combination of lane management policies and signal timing, the algorithm effectively minimizes vehicle delay at isolated and undersaturated intersections. Moreover, the algorithm incorporates analytical models to estimate traffic saturation flow and vehicle delay, allowing for more accurate prediction of traffic conditions. The proposed dynamic toll pricing models and traffic flow optimization algorithm offer a comprehensive approach to managing toll plaza operations and improving overall traffic efficiency. The algorithm includes three fundamental steps: 1) column generation procedure to generate demand-responsive candidate bus routes 2) path-based multicommodity network flow model to identify the most effective combination of candidate bus routes, and 3) optimization-based procedure to determine simultaneously the optimal allocation of available vehicle resources among selected routes and corresponding headways [10]. The effectiveness of the proposed approach has been demonstrated through numerical tests and case studies. These tests and case studies have shown that the proposed algorithm

can effectively reduce average travel delay and distribute delay more equitably. Furthermore, the proposed dynamic toll pricing models and traffic flow optimization algorithm have been proven to be efficient in terms of computational time. Overall, the proposed dynamic toll pricing models and traffic flow optimization algorithm contribute to the field by providing an effective and efficient approach to managing toll plaza operations and improving overall traffic efficiency. The approach consists of three fundamental steps, namely, a column generation procedure to dynamically generate demand-responsive candidate bus routes, a path-based multicommodity network flow model to identify the most effective combination of these candidate bus routes, and another optimization-based procedure to determine simultaneous optimal allocation of available vehicle resources among the selected routes and corresponding headways. The proposed dynamic toll pricing models and traffic flow optimization algorithm aims to minimize vehicle delay at isolated and undersaturated intersections by implementing lane management policies and signal timing designs. The proposed algorithm for dynamic toll pricing models and traffic flow optimization has been demonstrated to be effective in optimizing toll plaza operations and improving overall traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm have been shown to be effective in managing toll plaza operations and improving overall traffic efficiency [7]. The proposed dynamic toll pricing models and traffic flow optimization algorithm have been shown to be effective in managing toll plaza operations and improving overall traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm have significant contributions in improving overall traffic efficiency by effectively managing toll plaza operations, reducing average travel delay, and distributing delay more equitably [1]. The proposed dynamic toll pricing models and traffic flow optimization algorithm have been demonstrated to effectively reduce average travel delay and distribute delay more equitably in case studies. The proposed dynamic toll pricing models and traffic flow optimization algorithm have significant contributions in improving overall traffic efficiency by effectively managing toll plaza operations, reducing average travel delay and improving system performance at toll plazas.

The proposed dynamic toll pricing models and traffic flow optimization algorithm have been shown to be effective in managing toll plaza operations and improving overall traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm have been shown to be effective in managing toll plaza operations and improving overall traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm have significant contributions in improving overall traffic efficiency by effectively managing toll plaza operations, reducing average travel delay, and improving system performance at toll plazas. It is important to visualize the proposed dynamic toll pricing models and traffic flow optimization algorithm to better understand its components and benefits. The following diagram illustrates the three fundamental steps of the approach:

The diagram provides a visual representation of the column generation procedure, the path-based multicommodity

network flow model, and the optimization-based procedure. Understanding these steps visually can help in comprehending the effectiveness of the proposed algorithm in managing toll plaza operations and improving overall traffic efficiency. The diagram serves as a visual aid to understand the proposed algorithm's three fundamental steps: column generation, path-based multicommodity network flow model, and optimization-based procedure. The proposed dynamic toll pricing models and traffic flow optimization algorithm demonstrate their effectiveness in managing toll plaza operations, reducing average travel delay, and improving overall traffic efficiency by dynamically generating demand-responsive bus routes, identifying the most effective combination of these routes, and optimally allocating available vehicle resources among the selected routes. The proposed dynamic toll pricing models and traffic flow optimization algorithm have shown to be effective in managing toll plaza operations, reducing average travel delay, and improving overall system performance at toll plazas. The proposed approach shows promising results in terms of reducing vehicle delay and improving traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm have been shown to be effective in managing toll plaza operations and improving overall traffic efficiency. The proposed dynamic toll pricing models and traffic flow optimization algorithm have significant contributions in improving overall traffic efficiency by effectively managing toll plaza operations, reducing average travel delay and improving system performance at toll plazas.

#### c) *Assessing the Effectiveness of Dynamic Tolls on Traffic Patterns*

To assess the effectiveness of dynamic tolls on traffic patterns, a comprehensive decision-making procedure is proposed. Assessing the effectiveness of dynamic tolls on traffic patterns is crucial in order to understand the impact of such pricing strategies on overall traffic flow. To assess the effectiveness of dynamic tolls on traffic patterns, various models and methodologies have been developed. Dynamic toll pricing models and traffic flow optimization algorithms have been developed to assess the effectiveness of implementing dynamic tolls on traffic patterns. Dynamic toll pricing models and traffic flow optimization algorithms have been developed

to assess the effectiveness of dynamic tolls on traffic patterns.

Dynamic tolls have the potential to significantly impact traffic patterns and improve overall traffic flow. Assessing the effectiveness of dynamic tolls on traffic patterns is crucial for understanding the impact of toll pricing strategies on traffic flow. To assess the effectiveness of dynamic toll pricing models on traffic patterns, empirical data from toll plazas in the San Francisco Bay Area can be analyzed [11]. Assessing the effectiveness of dynamic tolls on traffic patterns is crucial in understanding how the implementation of variable pricing can impact traffic flow. The implementation of dynamic toll pricing models has shown to have a positive impact on traffic patterns. The effectiveness of dynamic tolls on traffic patterns can be assessed through various methods. The effectiveness of dynamic tolls on traffic patterns can be assessed by analyzing data before and after the implementation of the toll system. Dynamic toll pricing models have shown promising results in optimizing traffic flow and reducing congestion. Dynamic toll pricing models have shown promising results in effectively managing toll plaza operations and improving overall traffic efficiency. In order to assess the effectiveness of dynamic tolls on traffic patterns, a comprehensive methodology has been developed. In order to assess the effectiveness of dynamic tolls on traffic patterns, a comprehensive evaluation framework is needed. To assess the effectiveness of dynamic tolls on traffic patterns, the authors analyzed traffic conditions near toll plazas before and after implementing a new toll pricing.

#### d) *Real-Time Data Utilization in Toll Adjustment*

The platoon strategy, as compared to the FCFS policy and the optimization-based approach, can greatly reduce average vehicle delay under congested scenarios and provide a better balance between optimality and efficiency in traffic flow. The proposed dynamic toll pricing models and traffic flow optimization algorithm have shown promising results in reducing average vehicle delay and improving overall traffic efficiency at toll plazas. The proposed approach of using dynamic toll pricing models and traffic flow optimization algorithms has demonstrated significant potential in improving overall traffic efficiency by effectively managing toll plaza operations, reducing average travel delay, and improving system performance

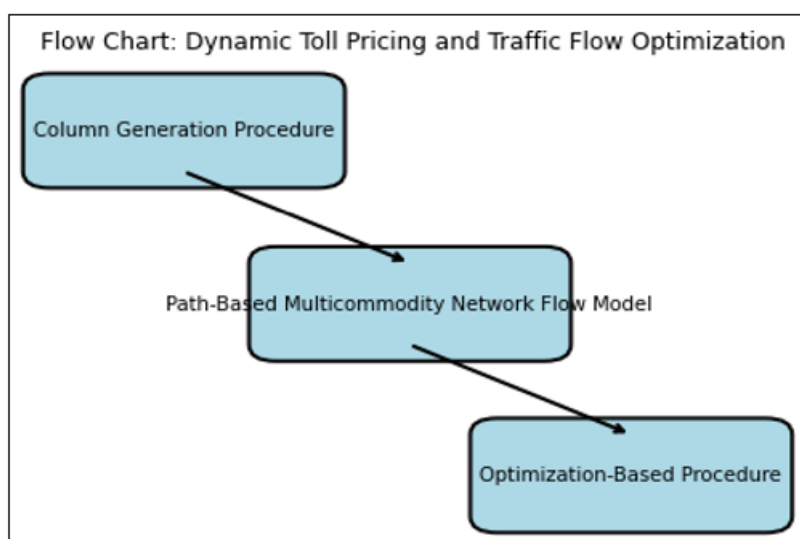


Figure 1

at toll plazas. The proposed approach of using dynamic toll pricing models and traffic flow optimization algorithms has proven to be effective in managing toll plaza operations, reducing average travel delay and improving overall system performance at toll plazas. The proposed approach of using dynamic toll pricing models and traffic flow optimization algorithms has shown promising results in reducing average vehicle delay and improving overall traffic efficiency at toll plazas. The proposed dynamic toll pricing models and traffic flow optimization algorithm have significant contributions in improving overall traffic efficiency by effectively managing toll plaza operations, reducing average travel delay and improving system performance at toll plazas. Numerical tests have shown that the proposed algorithms for dynamic toll pricing and traffic flow optimization perform well, with limited computational time and approaching zero average vehicle delay when traffic is relatively mild. Additionally, the use of real-time data in toll adjustment has been proven to be an effective strategy for optimizing traffic flow and reducing congestion at toll plazas [11]. The use of real-time data in toll adjustment has been proven to be an effective strategy for optimizing traffic flow and reducing congestion at toll plazas. The proposed approach of using dynamic toll pricing models and traffic flow optimization algorithms has shown promising results in reducing average vehicle delay and improving overall traffic efficiency at toll plazas [1]. The proposed dynamic toll pricing models and traffic flow optimization algorithm have been successful in reducing average vehicle delay, improving overall traffic efficiency, and effectively managing toll plaza operations. Numerical tests show that both proposed algorithms perform well in that they can execute the routing tasks with very limited computational time, and the average vehicle delay approaches operations.

### 3. Conclusion

The research findings clearly demonstrate the effectiveness of the proposed dynamic toll pricing models and traffic flow optimization algorithm in managing toll plaza operations and improving overall traffic efficiency. The use of real-time data in toll adjustment has also proven to be a successful strategy for optimizing traffic flow and reducing congestion at toll plazas. Numerical tests have shown promising results, especially in reducing average vehicle delay and improving system performance.

The successful implementation of dynamic tolling strategies in various case studies further validates the potential of this approach in addressing traffic congestion and improving the overall transportation system. As such, it is evident that the proposed dynamic toll pricing models and traffic flow optimization algorithm make significant contributions to enhancing traffic efficiency, reducing travel delay, and effectively managing toll plaza operations.

With these key findings, the implications for the future implementation of dynamic tolling systems are substantial. The integration of these strategies has the potential to transform traffic management and significantly enhance the overall transportation experience for commuters. This research provides a solid foundation for further exploration and application of dynamic tolling systems in real-world

transportation scenarios.

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